# Anisotropic Ejecta Distribution of Kilonova AT 2017gfo

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## ABSTRACT

Assuming that the ejecta produced during a binary neutron star merger is highly anisotropic, we propose an analytic model to fit the multi-wavelength data of AT 2017gfo, which is associated with the gravitational wave event GW170817. Our fitting results show that the observed data are consistent with the emission from a uniformly expanding ejecta with its mass and opacity anisotropically distributing with angle. The distribution of mass, velocity and opacity as functions of angle can be described by a cut-off power-law with different indices. The total mass of the ejecta is  $M_{\text{total}} \simeq 0.081 M_{\odot}$ . The derived velocity of the ejecta is  $v_{\text{ei}} \sim 0.27 c$  and the opacity  $\kappa$  ranges from 4.2 cm<sup>2</sup> g<sup>-1</sup> to 18 cm<sup>2</sup> g<sup>-1</sup>, both being consistent with the results from the numerical simulations in previous works. Our results suggest that radiation from the polar region of ejecta dominates over that from the equatorial region at both early and late times due to the anisotropic structure and viewing angle effect. We also show that the relativistic Doppler effect and equal-arrival-time surface play an important role in shaping the observed kilonova light curve due to the high speed of ejecta.

*Keywords:* stars: neutron – gravitational waves

## 1. INTRODUCTION

Shortly after [Hulse & Taylor](#page-10-0) [\(1975](#page-10-0)) discovered the first binary neutron star (BNS) system, considerable theories have pointed out that the merger of compact star binaries, neutron star-black hole (NS-BH), NS-NS ([Lattimer & Schramm](#page-10-1) [1976;](#page-10-1) [Symbalisty & Schramm](#page-10-2) [1982](#page-10-2)), can generate dynamical ejecta with enough high energy neutrons for heavy element (*A* ≳ 140) nucleosynthesis (*r-process*) [\(Metzger](#page-10-3) [2017,](#page-10-3) for review), completing the final puzzle of cosmic element origin. The rapid decay of the freshly synthesized lanthanide elements was later proposed to heat the BNS merger ejecta and produce a day-to-week luminous IR/optical/UV transient, which can be thousands of times brighter than no-vae, namely kilonova (KN) (Li & Paczyński [1998](#page-10-4); [Rosswog](#page-10-5) [2005;](#page-10-5) [Metzger et al.](#page-10-6) [2010](#page-10-6)). Such kilonove are naturally expected to be associated with short gamma-ray bursts (sGRB). However, only some indirect evidence ([Berger et al.](#page-10-7) [2005](#page-10-7); [Hjorth et al.](#page-10-8) [2005;](#page-10-8) [Tanvir et al.](#page-10-9) [2013\)](#page-10-9) was found during the past decades for such an association.

On August 17, 2017 at 12:41:04 UTC, the advanced LIGO/Virgo jointly detected a gravitational-wave event 40 Mpc away ([Abbott et al.](#page-10-10) [2017b\)](#page-10-10), which was later identified as a binary neutron star coalescence and named as GW170817. Merely 1*.*7 s after the trigger, an sGRB, GRB 170817A, was detected by both *Fermi* [\(Goldstein et al.](#page-10-11) [2017](#page-10-11); [Zhang et al.](#page-11-0) [2018](#page-11-0)) and *INTEGRAL* [\(Savchenko et al.](#page-10-12) [2017\)](#page-10-12) within the GW prediction area. About 11 hours after the trigger, several groups (first announced by [Coulter et al.](#page-10-13) [2017\)](#page-10-13) independently found an optical counterpart within the galaxy NGC 4993 and confirmed it to be a kilonova and named it as AT 2017gfo. The associated afterglow emission was later observed in X-ray and radio bands after several days (e.g. [Troja et al.](#page-10-14) [2017](#page-10-14); [Hallinan et al.](#page-10-15) [2017](#page-10-15)). Such four phenomena, i.e., a gravitational wave event, a gamma-ray burst, a kilonova, and a multi-wavelength afterglow, which were observed in an NS-NS merger event, have marked the beginning of multi-messenger time domain astronomy era (see [Abbott et al.](#page-10-16) [2017c,](#page-10-16) and references therein).

Both theoretical calculations and numerical simulations ([Hotokezaka et al.](#page-10-17) [2013;](#page-10-17) [Sekiguchi et al.](#page-10-18) [2015](#page-10-18); [Radice](#page-10-19) [et al.](#page-10-19) [2018b](#page-10-19)) have suggested that a fraction of matter  $(10^{-4} - 10^{-2} M_{\odot})$ , known as dynamical ejecta, should be tidally disrupted and ejected with speed  $v$   $\sim$  0*.*1−0*.3 c* (*c* is the speed of light) in several milliseconds during the BNS merger. The dynamical ejecta is initially neutron-rich with an electron fraction  $Y_e \sim 0.1 - 0.4$ . The electron fraction at the polar region of the ejecta will then increase to  $Y_e \gtrsim 0.3$  due to shock heating or weak interactions [\(Wanajo et al.](#page-10-20) [2014](#page-10-20); [Sekiguchi et al.](#page-10-18) [2015](#page-10-18); [Radice et al.](#page-10-21) [2016](#page-10-21)). Another source of ejecta originates in a neutrino-driven wind and viscositydriven outflow (hereafter referred as a secular component) from the remnant accretion disk and generally propagates with speed  $v \le 0.1$  *c* [\(Perego et al.](#page-10-22) [2014](#page-10-23); [Siegel et al.](#page-10-23) 2014;



<span id="page-1-1"></span>Figure 1. Schematic of our structured ejecta model. Colors represent the distribution of opacity *κ* from low (blue) to high (red). The viewing angle is  $\theta$ <sub>v</sub> and  $\omega$ ,  $\phi$  (not marked) are the co-altitude and azimuth in the observer frame respectively.

[Just et al.](#page-10-24) [2015](#page-10-24); [Martin et al.](#page-10-25) [2015](#page-10-25); [Wu et al.](#page-10-26) [2016](#page-10-26); [Fu](#page-10-27)[jibayashi et al.](#page-10-27) [2018](#page-10-27)). The evolution of KN ejecta thus leads to different regions with different *Ye*. Previous works have shown that using the "red" ( $Y_e \lesssim 0.3$ , higher opacity and lanthanide-rich) and "blue" (higher *Y<sup>e</sup>* and lanthanide-poor due to mild *r-process* nucleosynthesis) components can successfully explain the early IR/optical light curves (LC) and spectra [\(Cowperthwaite et al.](#page-10-28) [2017](#page-10-28); [Troja et al.](#page-10-14) [2017](#page-10-14); [Drout](#page-10-29) [et al.](#page-10-29) [2017](#page-10-29)) of AT 2017gfo. In addition, it has been realized that a third intermediate "purple" component is required to explain the additional week-to-month multi-wavelength data [\(Villar et al.](#page-10-30) [2017\)](#page-10-30). On the other hand, alternative approaches such as using a simplified semi-analytic anisotropic model of the ejecta [\(Perego et al.](#page-10-31) [2017\)](#page-10-31) or carefully considering the radiative transfer via a two-dimensional numerical simulation [\(Kawaguchi et al.](#page-10-32) [2018\)](#page-10-32) were attempted to relieve the apparent multi-component issue.

In this paper, we propose an anisotropic model with minimal physical assumptions and calculated resultant KN emission from the first principle. Similar to [Huang et al.](#page-10-33) [\(2018](#page-10-33)), we take into account a smooth distribution of the ejecta mass per solid angle, velocity and opacity as functions of jet angle. We also consider the Doppler effect and equal-arrival-time surface (EATS) in detail. Our model is described in [§2](#page-1-0). The fitting procedure between our model and data is described in §[3.](#page-2-0) The fitting results are then presented in §[4,](#page-3-0) followed by discussions and conclusions in [§5](#page-3-1).

## <span id="page-1-0"></span>2. THE KILONOVA MODEL

As illustrated in Figure [1](#page-1-1), the ejecta distribution is modeled by a cutoff power law function<sup>[1](#page-1-2)</sup>,

<span id="page-1-5"></span>
$$
F(\theta) = \begin{cases} F_0, & 0 < \theta \le \theta_0, \\ F_0 \left( \frac{\theta}{\theta_0} \right)^{\delta_F}, & \theta_0 < \theta < \pi/2, \end{cases}
$$
 (1)

where  $F = dM_{\text{ej}}/d\Omega$  or  $v_{\text{ej}}$  or  $\kappa_{\text{ej}}$  or  $T_c$  stands for either the angular distribution of ejecta mass *dM*ej*/d*Ω, velocity *v*ej, opacity  $\kappa_{ei}$  or temperature floor  $T_c$ . *F* reaches its extremum within  $\theta_0$ , which can be regarded as a "blue" component in the polar region, whereas *F* changes as a power law when *θ* approaches  $\pi/2$  which can be regarded as a "red" component in the equatorial region. As shown in [§4](#page-3-0), these continuous distributions can naturally lead to a smooth light curve without artificially introducing multiple components to explain the data.

According to [Korobkin et al.](#page-10-34) [\(2012](#page-10-34)), the input radioactive energy rate is proportional to the *r-process* mass, so we have

<span id="page-1-6"></span>
$$
\frac{dL_{\rm in}}{d\Omega}(t,\theta) = 4 \times 10^{18} \frac{dM_{\rm ej}}{d\Omega} \left[ 0.5 - \frac{1}{\pi} \arctan\left(\frac{t - t_0}{\sigma}\right) \right]^{1.3} \text{ erg s}^{-1},\tag{2}
$$

where  $t_0 = 1.3$  s and  $\sigma = 0.11$  s are empirical constants. However, not all the radioactive energy could be converted to power KN. The cross section of the ejecta material to high energy *γ*−rays, neutrinos and particles created by decay process can introduce a thermalization efficiency  $\epsilon_{th}$ . [Barnes et al.](#page-10-35) ([2016\)](#page-10-35) provides an empirical equation:

<span id="page-1-3"></span>
$$
\epsilon_{\text{th}}(t,\theta) = 0.36 \left[ e^{-at} + \frac{\ln(1+2bt^d)}{2bt^d} \right],
$$
 (3)

where *a*, *b*, and *d* are constants related to the ejecta mass, velocity and the magnetic fields of the merger object and are listed as Table 1 in [Barnes et al.](#page-10-35) [\(2016](#page-10-35)). We find that such a table can be successfully fitted by the following empirical function, 0*.*2

<span id="page-1-4"></span>
$$
a, b = c_1 + c_2 (v_{\rm ej} - c_3) e^{-(c_4 m_{\rm ej})^{0.2}}
$$
  
\n
$$
d = c_1 + c_2 v_{\rm ej} + c_3 m_{\rm ej}
$$
\n(4)

where  $c_i$  are free parameters, which are listed for  $a$ ,  $b$  and *d* in Table [1](#page-2-1). We note that  $m_{ej}$  in Eq.[3](#page-1-3) and Eq.[4](#page-1-4) is the total mass within a homologous photosphere while the ejecta mass in our model represents the angular density per solid angle. Thus, a factor of  $4\pi$  should be multiplied to obtain the equivalent spherical mass when calculating the efficiency in Eq[.3](#page-1-3).

After obtaining the input energy and thermal efficiency, the bolometric luminosity can be calculated following [Arnett](#page-10-36)

<span id="page-1-2"></span><sup>&</sup>lt;sup>1</sup> We have also investigated other distributions such as  $F(\theta) = \exp(\alpha \theta^2)$ and  $F(\theta) = (1 + \theta/\theta_0)^{\delta_F}$ , while both were disfavored by fitting results.

Table 1. *a, b, d* FITTING PARAMETERS

<span id="page-2-1"></span>

c <sub>1</sub>	c <sub>2</sub>	$c_3$	$c_4$
	$b \mid 0.121$ 92.3	$7.16 \times 10^{-2}$ $2.52 \times 10^{5}$	
$d \mid 0.724$	7.57	2.55	

[\(1980,](#page-10-36) [1982\)](#page-10-37) and [Chatzopoulos et al.](#page-10-38) [\(2012\)](#page-10-38):

$$
\frac{dL_{\text{bol}}}{d\Omega} = e^{-(t/t_d)^2} \int_0^t \frac{dL_{\text{in}}}{d\Omega} \epsilon_{\text{th}} \, e^{(t'/t_d)^2} \frac{2t'}{t_d^2} dt',\tag{5}
$$

where  $t_d = \sqrt{2\kappa m_{\text{ej}}/\beta v c}$  is the geometric mean diffusion timescale with general density profile constant  $\beta$  = 13.8. The radiation can be approximately described by a blackbody spectrum with effective temperature T,

$$
\frac{dL_{\text{bol}}}{d\Omega}(t,\theta) = (v_{\text{ej}}t)^2 \sigma_{\text{SB}} T^4(t,\theta). \tag{6}
$$

Numerical simulations ([Barnes & Kasen](#page-10-39) [2013\)](#page-10-39) indicate that a critical temperature exists at which the ejecta temperature stops further decrease. This can be related to the lanthanide abundance and their first ionization temperature. Hence we assume this temperature floor also complies with Eq[.1](#page-1-5) distribution and the photosphere temperature can be written as

$$
T_{\text{phot}}(t,\theta) = \begin{cases} T(t,\theta), & T \leq T_c, \\ T_c(\theta), & T > T_c. \end{cases} \tag{7}
$$

The exact photosphere radius is derived accordingly by

$$
R_{\text{phot}}(t,\theta) = \begin{cases} v_{\text{ej}}t, & T \leq T_c, \\ \left(\frac{T}{T_c}\right)^2 v_{\text{ej}}t, & T > T_c. \end{cases}
$$
(8)

As shown in Figure [1,](#page-1-1) the polar angle in the source frame *θ* can be rewritten as a function of the co-altitude *ω* and azimuth  $\phi$  in the observer frame, which is used in further calculations,

<span id="page-2-2"></span>
$$
\theta(\phi,\omega) = \arccos(\cos\theta_v \cos\omega - \sin\theta_v \sin\omega \cos\phi). \tag{9}
$$

As the ejecta velocity (*∼* 0*.*3 *c*, [Villar et al.](#page-10-30) [2017;](#page-10-30) [Perego](#page-10-31) [et al.](#page-10-31) [2017\)](#page-10-31) reaches the sub-relativistic regime, the Doppler effect should be taken into account to calculate the observed energy flux. Following Eq.(4.110) in [Rybicki & Lightman](#page-10-40) [\(2008\)](#page-10-40), we have

$$
\frac{I(\nu_o)}{\nu_o^3} = \frac{B(\nu_s, T)}{\nu_s^3},\tag{10}
$$

where  $\nu$ <sup>*o*</sup> is the frequency corresponding to the central wavelength of a given band in the observer frame, *ν<sup>s</sup>* is the emitted frequency in the ejecta frame, and  $B(\nu, T)$  is the Planck function, i.e.,

$$
B(\nu, T) = \frac{2h\nu^3}{c^2} \frac{1}{e^{h\nu/kT} - 1}.
$$

The observed frequency is

<span id="page-2-4"></span>
$$
\nu_o = \frac{\nu_s}{\Gamma(1 - \beta \cos \omega)},\tag{11}
$$

<span id="page-2-5"></span>where  $\beta = v_{\text{ej}}(\theta)/c$ ,  $\Gamma = 1/\sqrt{1-\beta^2}$  and  $\omega$  is introduced in Eq[.9](#page-2-2). Thus  $ν_s = \Gamma(1 - \beta \cos \omega) v_o$  is a function of  $(θ, ω)$  and we could get the observed intensity  $I(\nu_o)$  in each band.

Finally, similar to Eq.4&5 in [Martin et al.](#page-10-25) [\(2015](#page-10-25)), we obtain the observed flux density by integrating over the EATS of the ejecta that is moving towards the observer,

$$
\mathcal{F}(\nu_o, t_o) = \iint_{\text{semisphere}} I(\nu_o) \frac{R_{\text{phot}}^2(t', \theta)}{D_L^2} \cos \omega \, d\Omega'
$$
  
\n
$$
= \frac{\nu_o^3}{D_L^2} \iint_{\text{semisphere}} B(\nu_s(\theta, \omega), T_{\text{phot}}(t', \theta)) \frac{R_{\text{phot}}^2(t', \theta) \cos \omega}{\nu_s^3(\theta, \omega)} d\Omega',
$$
\n(12)

where *t'* is a function of  $(\theta, \omega, t_o)$  given by EATS, and  $D_L$ is the distance to the source and we adopt  $D_L = 43.8$  Mpc, according to [Abbott et al.](#page-10-41) ([2017a](#page-10-41)).

#### 3. DATA AND FIT

# 3.1. *The Unified Dataset*

<span id="page-2-0"></span>The multi-wavelength light curve data are taken from Table 3 in [Villar et al.](#page-10-30)  $(2017)$  $(2017)$  and the open kilonova catalog<sup>[2](#page-2-3)</sup>. The data set is a collection of observations originally presented in [Andreoni et al.](#page-10-42) [\(2017\)](#page-10-42); [Arcavi et al.](#page-10-43) [\(2017\)](#page-10-43); [Coulter et al.](#page-10-13) ([2017\)](#page-10-13); [Cowperthwaite et al.](#page-10-28) [\(2017](#page-10-28)); [Díaz et al.](#page-10-44) ([2017\)](#page-10-44); [Drout](#page-10-29) [et al.](#page-10-29) ([2017\)](#page-10-29); [Evans et al.](#page-10-45) ([2017\)](#page-10-45); [Hu et al.](#page-10-46) [\(2017](#page-10-46)); [Valenti](#page-10-47) [et al.](#page-10-47) ([2017](#page-10-47)); [Kasliwal et al.](#page-10-48) ([2017\)](#page-10-48); [Lipunov et al.](#page-10-49) ([2017\)](#page-10-49); [Pian et al.](#page-10-50) ([2017\)](#page-10-50); [Pozanenko et al.](#page-10-51) [\(2018](#page-10-51)); [Shappee et al.](#page-10-52) ([2017\)](#page-10-52); [Smartt et al.](#page-10-53) [\(2017](#page-10-53)); [Tanvir et al.](#page-10-54) ([2017\)](#page-10-54); [Troja et al.](#page-10-14) ([2017\)](#page-10-14); [Utsumi et al.](#page-10-55) [\(2017](#page-10-55)), with all upper limits and W band data excluded. For simplicity, we only take the data measured in AB magnitude. Upper limits and unfiltered data are not taken into account. Extinction caused by the Milky Way was corrected following [Fitzpatrick](#page-10-56) [\(1999](#page-10-56)).

# 3.2. *Fitting Procedure*

Our model (Eq.[12\)](#page-2-4) is then fitted to the observational data using a Markov Chain Monte Carlo approach. A Python package, emcee ([Foreman-Mackey et al.](#page-10-57) [2013\)](#page-10-57), is utilized for sampling and getting posterior predictions on our model parameters.

<span id="page-2-3"></span><sup>2</sup> <http://kilonova.space/>

<span id="page-3-6"></span>

<span id="page-3-2"></span><sup>a</sup>Calculated with the  $\sigma$  term in Eq[.13](#page-3-3).

The log-likelihood function is defined as

$$
\ln \mathcal{L} = -\frac{1}{2} \sum_{i=1}^{n} \left[ \frac{(O_i - M_i)^2}{\sigma_i^2 + \sigma^2} + \ln \left( 2\pi (\sigma_i^2 + \sigma^2) \right) \right],
$$
 (13)

where *n* is the total number of observation points (in our case,  $n = 557$ ),  $O_i$ ,  $M_i$ ,  $\sigma_i$  are the *i*th observed magnitude, modeled magnitude and observed uncertainty. We also introduce a scatter term,  $\sigma$ , to account for any additional systematic error.  $\sigma$  is treated as a free parameter during the fit.

There are ten free parameters in our model, namely,  $(1) m_0$ , initial (polar region) value of ejecta mass per solid angle, (2)  $v_0$ , ejecta velocity at polar region, (3)  $\kappa_0$ , opacity at polar region, (4)  $T_c$ , temperature floor at polar region, (5)  $\delta_m$ , power law index of mass distribution, (6)  $\delta_{\nu}$ , power law index of velocity distribution, (7)  $\delta_{\kappa}$ , power law index of opacity distribution, (8)  $\delta_T$ , power law index of temperature distribution, (9)  $\theta_0$ , critical angle, and (10)  $\sigma$ , systematic error term.

The priors of  $m_0$ ,  $\kappa_0$ ,  $T_c$  and  $\delta_v$  are set to be log-uniform because they may spread several orders of magnitude with changing power-law indices and critical angle<sup>[3](#page-3-4)</sup>. The other parameters are all set with flat priors. The viewing angle is fixed to  $\theta_{\rm v}$  = 30<sup>°</sup> [\(Abbott et al.](#page-10-10) [2017b](#page-10-10); [Hajela et al.](#page-10-58) [2019\)](#page-10-58).

We then run *emcmc* for  $n_{\text{walkers}} \times n_{\text{steps}} = 100 \times 11600$ . To check the convergence of our chains, we follow the emcee documentation<sup>[4](#page-3-5)</sup> and perform an autocorrelation analysis. The estimated integrated autocorrelation time *τ<sup>f</sup>* is less than 230 for all 10 parameters, meaning this can be considered as a reliable estimation because  $n_{\text{steps}}/\tau_f > 50$ . Thus we could safely discard the first 4000 steps, treating them as burn-in phase.

### 4. RESULTS

<span id="page-3-0"></span>The best-fit model is over-plotted with the observed data in Figure [2.](#page-5-0) Constraints on parameters are shown in Table [2](#page-3-6) and Figure [3.](#page-6-0) In Figure [4](#page-7-0) we plot the angular distributions of ejecta mass, velocity, opacity and temperature of our best-fit model.

Based on our results, we get the total mass of the ejecta  $M_{\text{total}} \simeq 0.081 M_{\odot}$  by integrating over the sphere. In order <span id="page-3-3"></span>to compare with previous researches (e.g., [Villar et al.](#page-10-30) [2017](#page-10-30)), we also define a "blue" region (or the polar region) of which ejecta polar angle  $\theta \leq \theta_0$  and a "red" region (or the equatorial region) for the ejecta with the polar angle  $\theta_0 < \theta \le 90^\circ$ . And the mass of the blue region is  $M_{blue} \sim 0.010 M_{\odot}$ . The high ejecta velocity  $v_{ei} = 0.276$  *c* and its corresponding powerlaw index  $log(-*δ*<sub>v</sub>) = −3.835$  indicate a flat velocity distri-bution, as shown in Figure [4](#page-7-0). The opacity  $\kappa_{ei}$  ranges from  $\sim$  4.2 cm<sup>2</sup> g<sup>-1</sup> at the polar region to  $\sim$  18 cm<sup>2</sup> g<sup>-1</sup> at the equatorial plane. And the temperature floor  $T_c$  decreases from *∼* 3800 K to *∼* 200 K as *θ* increases. During the time interval we investigated ( $t \le 26$  day), the ejecta within  $\theta \le 80^\circ$ has cooled to its corresponding temperature floor ( $T_c \approx 550 \text{ K}$ at  $\theta \approx 80^\circ$ ). As polar angle further increases, the actual temperature begins to rise and reaches  $T \approx 800 \text{ K}$  at  $\theta = 90^\circ$ .

In Figure [5](#page-8-0) we compare our model-predicted spectral energy distribution (SED) with the observed data at different times, which again shows our modeling successfully reproduced the spectral evolution of the kilonova emission.

To compare our results with [Villar et al.](#page-10-30) ([2017\)](#page-10-30), we plot the calculated blue and red component of our model of each individual band in Figure [6.](#page-9-0) The blue curves represent the emission from the polar region, red curves from the equatorial region and black curves are the sum of these two components. Our results are consistent with [Villar et al.](#page-10-30) ([2017\)](#page-10-30) in terms of the peak time of the blue and red components. However, our results show that the blue component still dominates the emission at a late time, likely due to the introudced anisotropic structure of the ejecta. This can be seen in Figure [1,](#page-1-1) where an observer at  $\theta$ <sup>*v*</sup> = 30<sup>°</sup> will naturally receive more radiation from polar region. The equatorial component will dominate at late time only when the viewing angle is large enough (e.g.,  $\theta_v = 90^\circ$ ). Additionally, the distribution of  $T_c$  in our model is different. The blue component in our model has higher temperature floor, while in [Villar et al.](#page-10-30) [\(2017](#page-10-30))  $T_c$  of red & purple components are higher.  $T_c$  is a factor that "controls" the allocation of energy into different bands for a given *L*bol determined in Eq.[5,](#page-2-5) which can lead the light curves to behave differently.

## 5. DISCUSSIONS & SUMMARY

<span id="page-3-1"></span>We have successfully modeled the multiwavelength light curves of the kilonova AT 2017gfo by utilizing an anisotropic ejecta distribution of the ejecta and yield the following main

<span id="page-3-4"></span><sup>&</sup>lt;sup>3</sup> During the fitting process, we firstly limit  $\delta$ <sup>*v*</sup> to be negative and use a flat prior. While the results show  $\delta$ <sup>*v*</sup>  $\approx$  0, so we use a log-uniform prior (i.e., a flat log(−*δv*)) instead to better investigate its distribution.

<span id="page-3-5"></span><sup>4</sup> <https://emcee.readthedocs.io/en/latest/tutorials/autocorr/>

conclusions: (1) we find a cutoff power law model in the ejecta structure fits best to the observed data. (2) Our bestfitting model leads to a uniformly expanding photosphere with  $M_{\text{total}} \simeq 0.081 M_{\odot}$  (among which  $\sim 0.010 M_{\odot}$  from polar region and the else from equatorial region),  $v_{ei} \sim 0.27$  *c* and opacity 4.2 cm<sup>2</sup>  $g^{-1} \lesssim \kappa_{ej} \lesssim 18$  cm<sup>2</sup>  $g^{-1}$ . (3) Our modeling coincides with dynamical ejecta moving at *v ≈* 0*.*2−0*.*3 *c*, in which case the relativistic Doppler effect and EATS play an important role in shaping the observed light curve. (4) We find although the mass of the polar region is only a small fraction of the total mass, emission from the polar region dominates at later time for most bands, which is mainly caused by the anisotropic structure when viewed from the polar direction and the influence of a different  $T_c$  distribution which is higher at the polar region.

We have noticed that the total ejecta mass in our model  $M_{\text{total}} \simeq 0.081 M_{\odot}$ , although consistent with some of the previous results [\(Villar et al.](#page-10-30) [2017;](#page-10-30) [Perego et al.](#page-10-31) [2017](#page-10-31)) in general, is still significantly higher than the mass of the dynamical and secular components predicted in a series of recent numerical simulations (e.g., [Hotokezaka et al.](#page-10-17) [2013](#page-10-17); [Martin et al.](#page-10-25) [2015](#page-10-25); [Fujibayashi et al.](#page-10-27) [2018;](#page-10-27) [Radice et al.](#page-10-19) [2018b\)](#page-10-19). Our results thus suggest that additional central power from the central engine is needed. Possible sources of such power include the nebular wind ([Ren et al.](#page-10-59) [2019\)](#page-10-59) and hybrid energy input by a long-lived remnant ([Yu et al.](#page-11-1) [2018](#page-11-1); [Li et al.](#page-10-60) [2018](#page-10-60)). The central engine could be further constrained with the help of afterglows in future events [\(Xiao et al.](#page-11-2) [2017;](#page-11-2) [Liu et al.](#page-10-61) [2020](#page-10-61)). Furthermore, the ejecta mass in our results is also subject to some ignorance of the physical details such as the direction preference of photon diffusion ([Kawaguchi et al.](#page-10-32) [2018](#page-10-32)) in realistic radiation transfer calculations and that the coefficient in Eq.[2](#page-1-6) may change under different conditions (see [Perego](#page-10-31) [et al.](#page-10-31) [2017](#page-10-31) and references therein). Those aspects have not been taken into account due to the limited scope of this study.

The uniform distribution of the high velocity in our results is consistent with the property of a dynamical ejecta in previous studies ([Sekiguchi et al.](#page-10-18) [2015;](#page-10-18) [Radice et al.](#page-10-19) [2018b](#page-10-19)). The higher dynamical ejecta mass in our results suggests additional components such as secular and viscous-dynamical components [\(Perego et al.](#page-10-31) [2017](#page-10-31); [Radice et al.](#page-10-62) [2018a](#page-10-62); [Fu](#page-10-27)[jibayashi et al.](#page-10-27) [2018](#page-10-27)) should be considered in future work. The best-fit of the opacity for the blue component is slightly higher than what was previously thought ([Tanaka et al.](#page-10-63) [2018\)](#page-10-63) but still consistent with a recent case study ([Tanaka et al.](#page-10-64) [2019\)](#page-10-64).

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<span id="page-5-0"></span>Figure 2. Multiwavelength observations of AT 2017gfo accompanied with our best-fit model. The magnitude values have already been corrected for extinction. *K* band and *K<sup>s</sup>* band data are treated with the same central wavelength.



<span id="page-6-0"></span>Figure 3. Corner plot illustrating posterior probability of our model. The strong correlation between  $\theta_0$  and  $\delta_m$  is a natural result because both of them could control the changing slope of mass distribution. The flat distribution of log(−*δv*) provides a rough lower limit *δ<sup>v</sup>* ≳ −10<sup>−</sup><sup>2</sup> .



<span id="page-7-0"></span>Figure 4. Distributions of ejecta physical properties as a function of polar angle *θ*. Panels from left to right are integrated mass (only semisphere,  $\times$ 2 to get the total mass), velocity, opacity and temperature floor. Black lines are the best-fitting model and green shades depict the  $1\sigma$  uncertainties.



<span id="page-8-0"></span>Figure 5. Time evolution of observed SED and our model results. The data are categorized via *K-means* clustering. Each curve is shifted down by 0*.*1 dex compared with the previous curve.



<span id="page-9-0"></span>Figure 6. Observed and modeled LC in selected bands. Blue lines represent emission from polar region, red lines from equatorial region and black lines are the sum of of these two components. Observed magnitudes are shown in blue dots. The bottom panel of each subplot shows the residual.

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